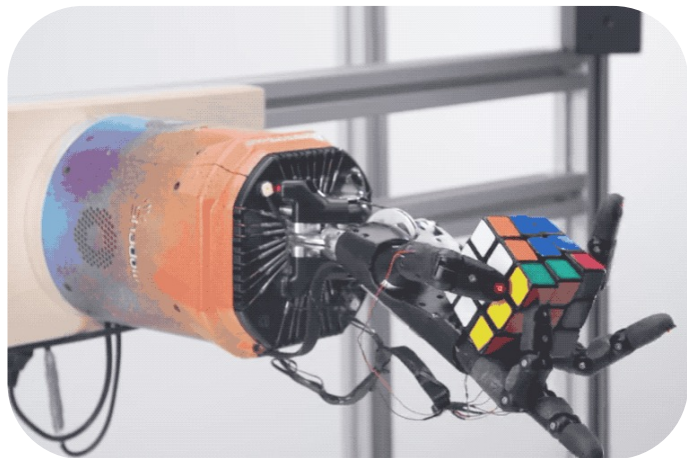


Safety Guarantees for Uncertain Systems in Interactive Settings

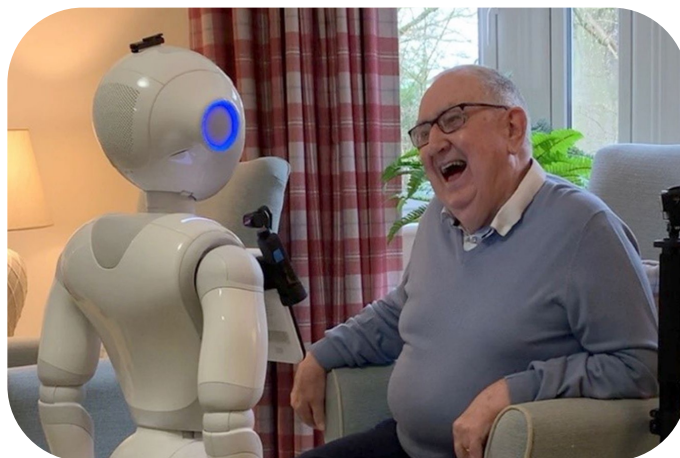


Kai-Chieh Hsu

April 29, 2021



OpenAI: Dactyl



Softbank robotics / RobotLAB: Pepper



Tesla: self-driving car



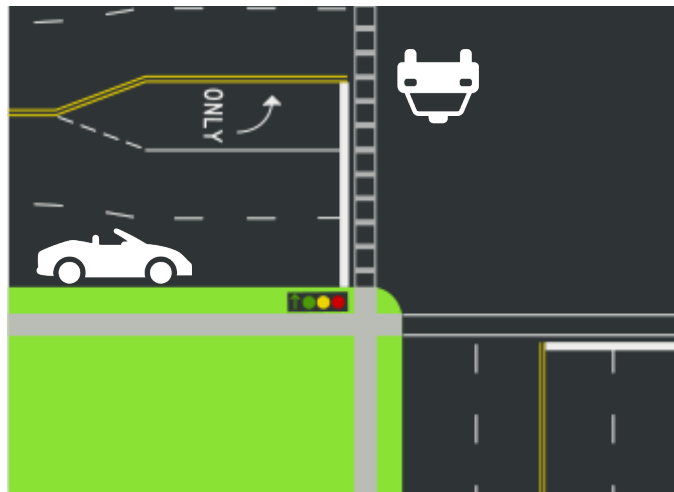
NY Times: Boeing 737



Uber car accident

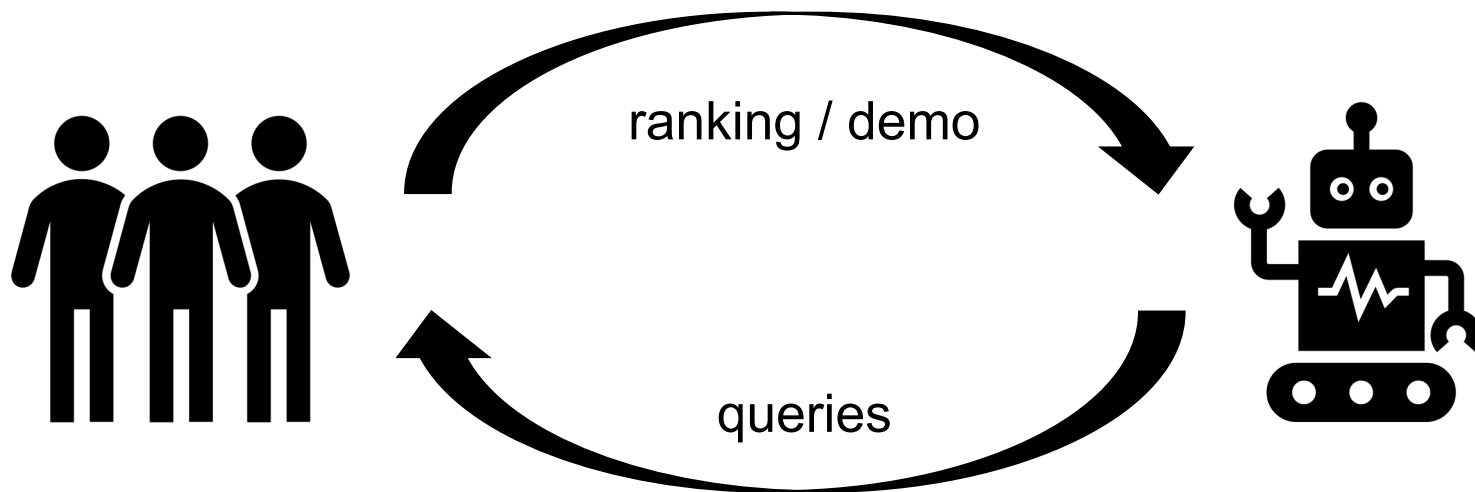


OpenAI: Reward Hacking



How to provide **safety guarantees** for **uncertain** systems?

How to **loop humans in** to better understand their preference?



Outline

- Introduction
- Supervisory control in high-dimensional systems
- Inverse specification
- Conclusion and future works

Supervisory Control: Shielding

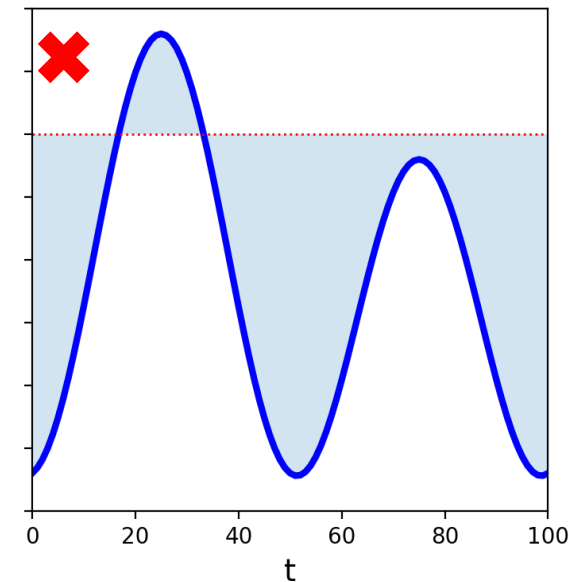
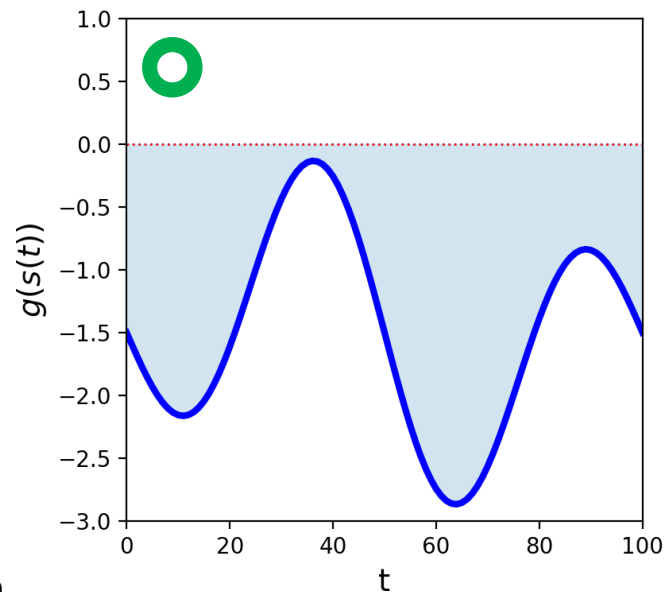
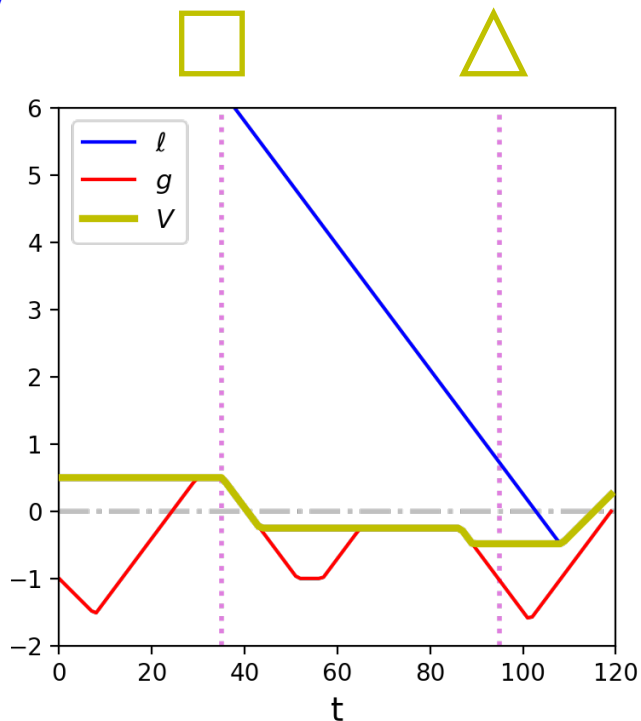
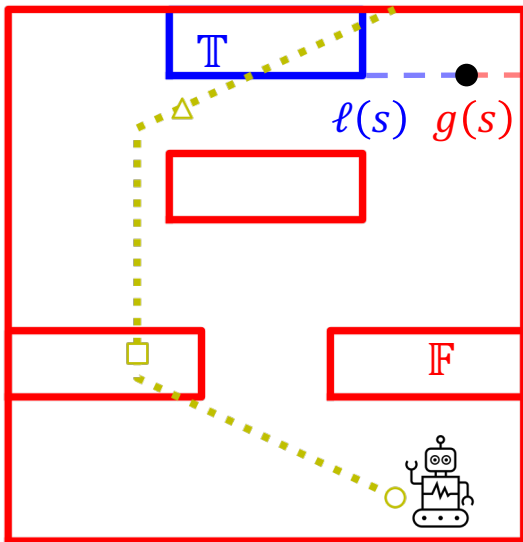
An approximate method to provide **fallback control** to high-dimensional systems



Keep **safe** away from forbidden states but
maintain **liveness** to reach target states

$s \in \mathbb{T} \leftrightarrow \ell(s) \leq 0$: reachability

$s \in \mathbb{F} \leftrightarrow g(s) > 0$: safety



Dynamics: $\dot{s} = f(s, u)$

Goal: find u such that

$\exists t, s(t) \in \mathbb{T} \wedge \forall \tau \in [0, t], s(\tau) \notin \mathbb{F}$

Reach-Avoid (RA)

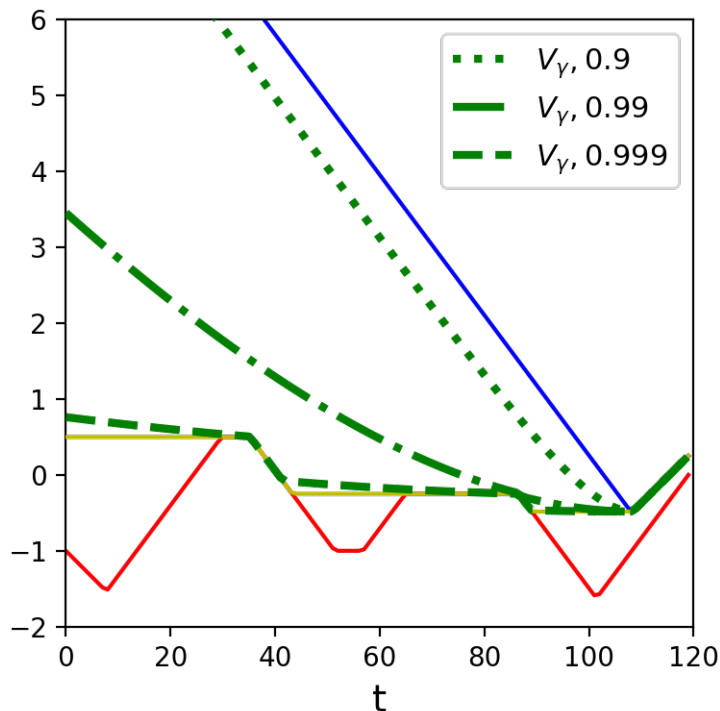
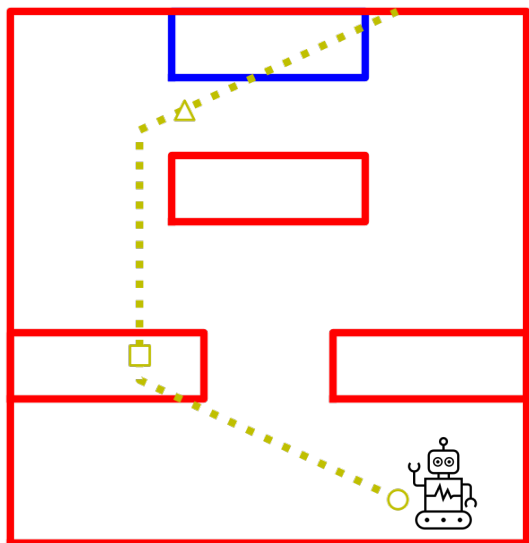
$$L(s^u) = \min_{t \in [0, T]} \max\{\ell(s(t)), \max_{\tau \in [0, t]} g(s(\tau))\}$$

$$V(s) = \min_u L(s^u) = \max\{g(s), \min\{\ell(s), \min_u V(s + f(s, u)\Delta t)\}\}$$

Sum of costs, Lagrange

$$L(s^u) = \sum_{t=0}^T c(s(t))$$

$$V(s) = \min_u L(s^u) = \min_u c(s, u) + V(s + f(s, u)\Delta t)$$



Goal: find u such that

$$\exists t, \mathbf{s}(t) \in \mathbb{T} \wedge \forall \tau \in [0, t], \mathbf{s}(\tau) \notin \mathbb{F}$$

Reach-Avoid Bellman Equation:

$$V(s) = \max \left\{ g(s), \min \left\{ \ell(s), \min_u V(s_+^u) \right\} \right\}$$

$s_+^u := s + f(s, u)\Delta t$

 **Curse of dimensionality** → deep RL

Lagrange or SUM

$$L(\xi) = \sum_t \gamma^t c(\xi(t))$$

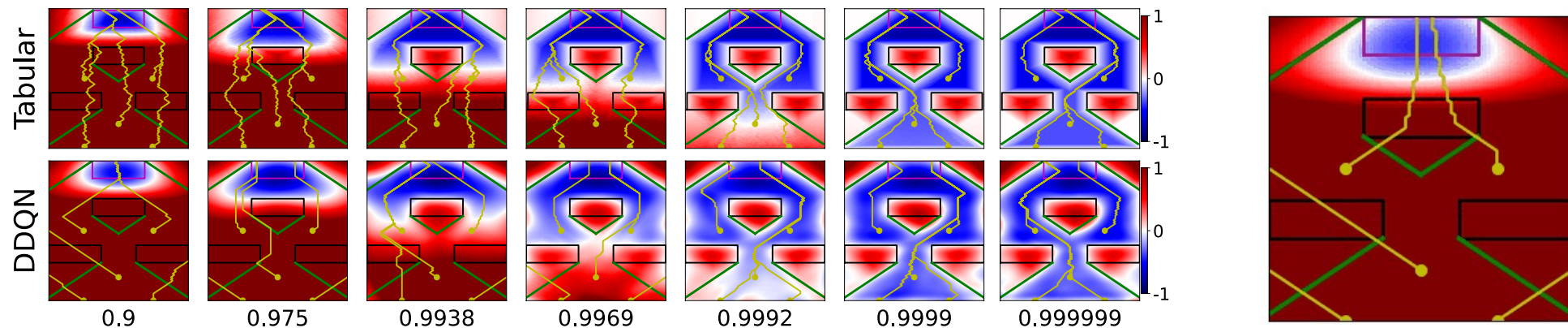
$$V(s) = \min_u \gamma (c(s, u) + V(s_+^u)) + (1 - \gamma)c(s, u)$$

Discounted Reach-Avoid Bellman Equation:

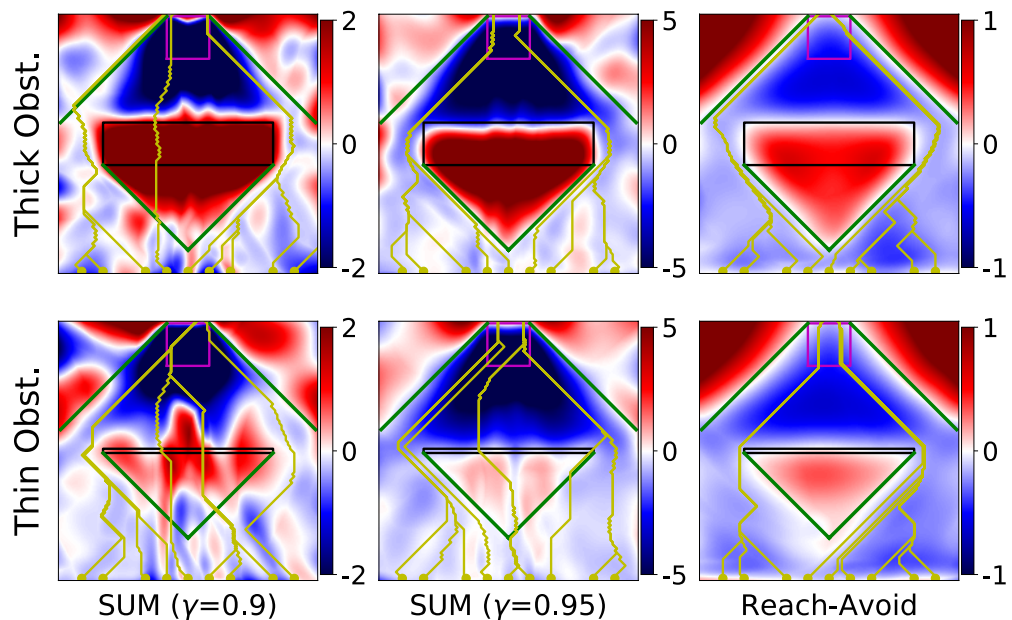
$$V_\gamma(s) = \gamma \max \left\{ g(s), \min \left\{ \ell(s), \min_u V(s_+^u) \right\} \right\} + (1 - \gamma) \max \{ g(s), \ell(s) \}$$

Double Deep Q-Network

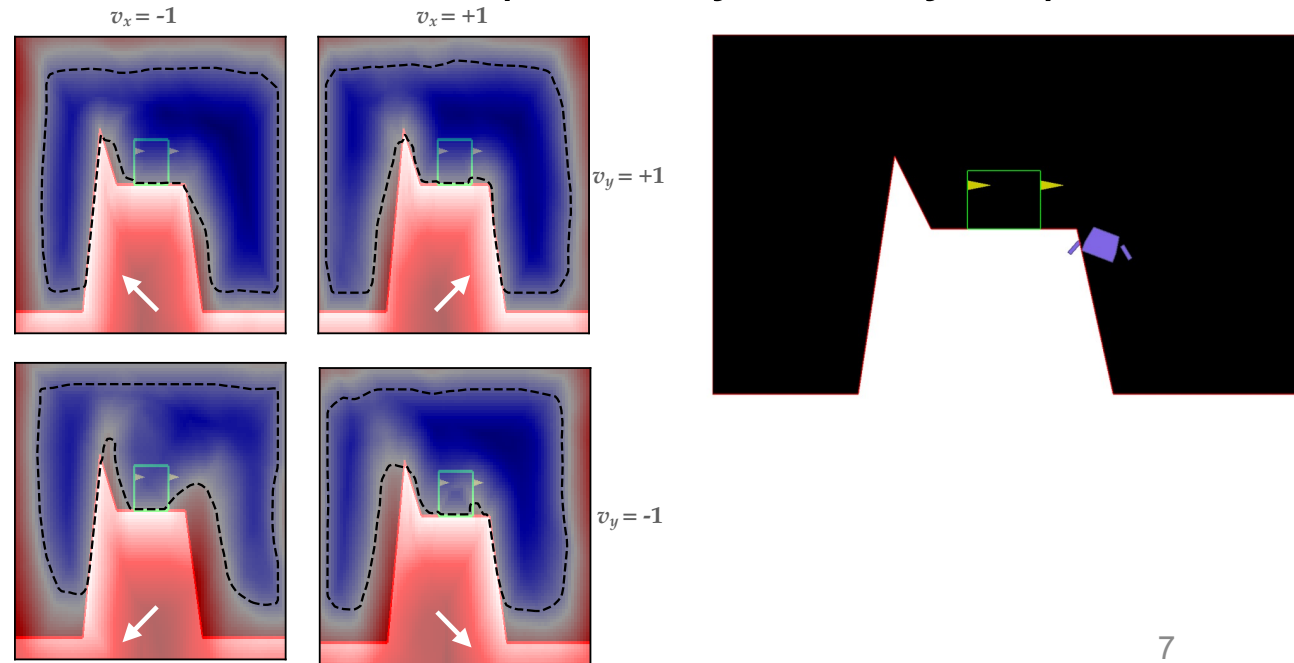
Conservativeness of Discounted Reach-Avoid Set



Reach-Avoid vs. Lagrange



Lunar Lander (6D: $x, y, \theta, \dot{x}, \dot{y}, \dot{\theta}$)

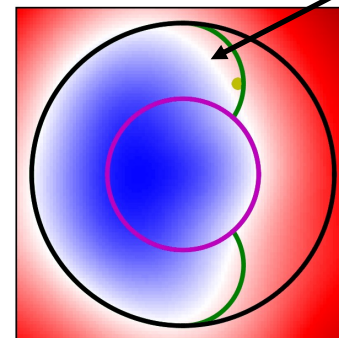


Untrusted Oracles

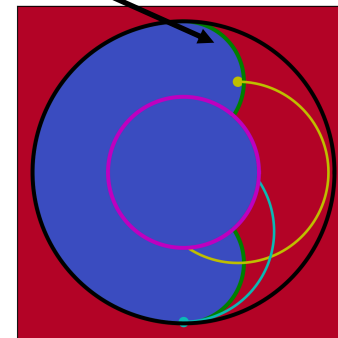
Dubins Car

- State: x-pos, y-pos, heading angle
- Actions: straight, left turn and right turn

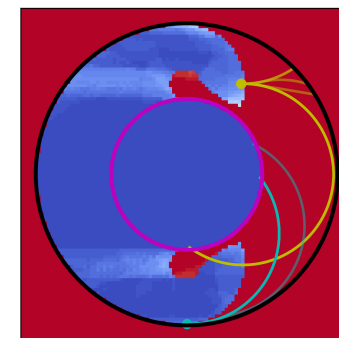
Approximation error!



Value Function



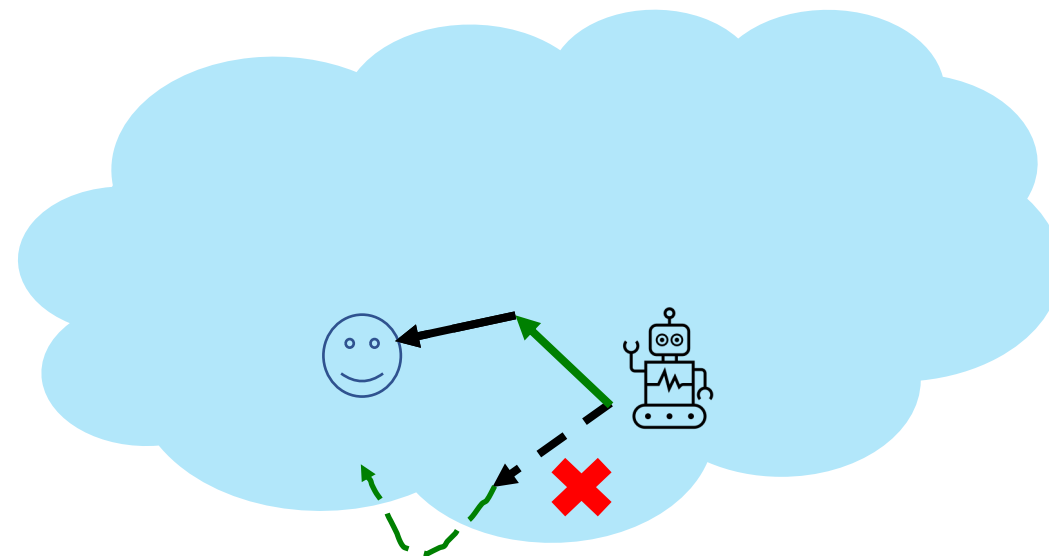
Analytic



Rollout

Shielding scheme:

- obtain a candidate action
- simulate a short trajectory forward
- if not, reach-avoid action
- if remaining in the reach-avoid set, we execute the candidate action

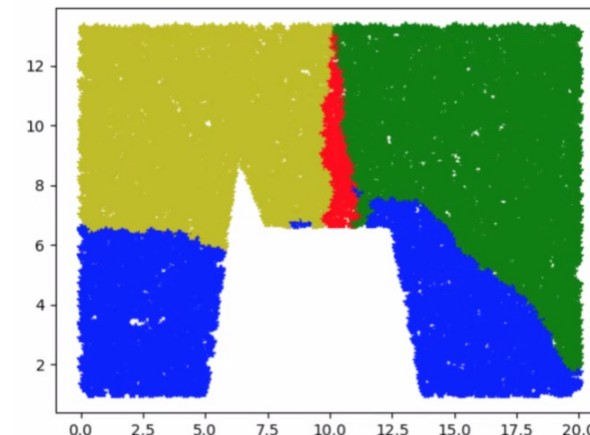


Future Works

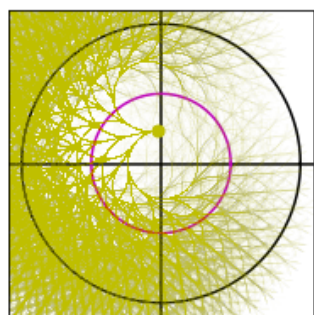
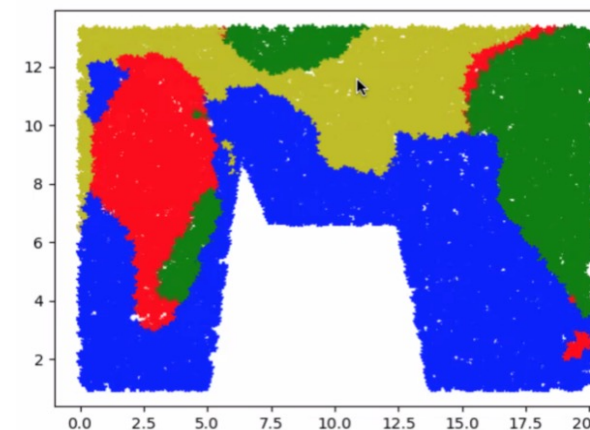
- Learned policy degrades in the no-discount limit
 - LL's actions: **Right**, **Left**, **Main thruster on**, **Thruster off**
 - Actor-Critic algorithms, e.g., soft actor-critic
- Zero-sum differential game
 - $V(s) = \max \left\{ g(s), \min \left\{ \ell(s), \min_u \max_d V(s_+^{u,d}) \right\} \right\}$
 - Principle of iterative adversarial improvements

$$\theta = \dot{x} = \dot{y} = \dot{\theta} = 0$$

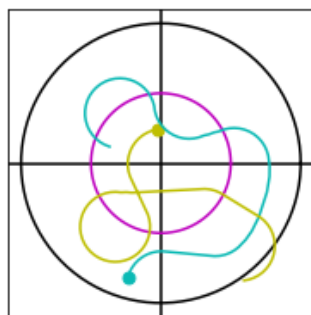
$$\gamma = 0.99$$



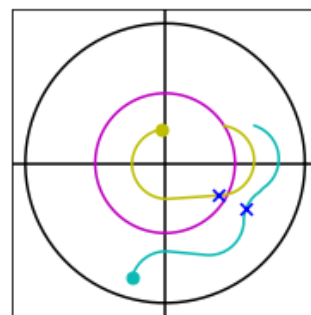
$$\gamma = 0.9999$$



Exhaustive Search



Rollout: -0.145



Exhaustive: 0.13

Attacker
Defender

Future Works

- Unknown Environment Exploration: PAC-Bayes Control framework

- Assumption:

- An underlying distribution D of environments
- We have a set of N sample environments, S

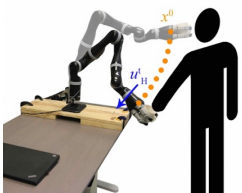
- PAC-Bayes Bound: with probability $1 - \delta$,

$$C_D(P) \leq C_S(P) + \text{Reg}(P, P_0)$$

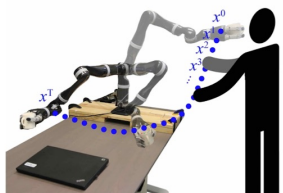
$$\text{Reg}(P, P_0) = \sqrt{\left(\frac{KL(P || P_0) + \log\left(\frac{2\sqrt{N}}{\delta}\right)}{2N} \right)}$$

- How can we add shielding to improve the bound?

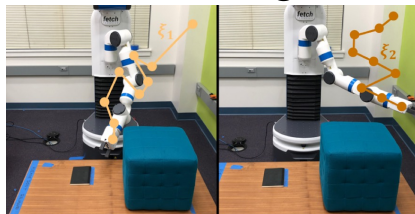
Correction



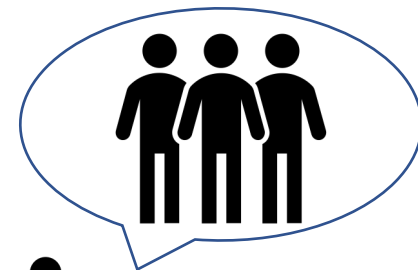
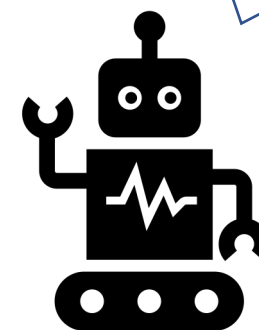
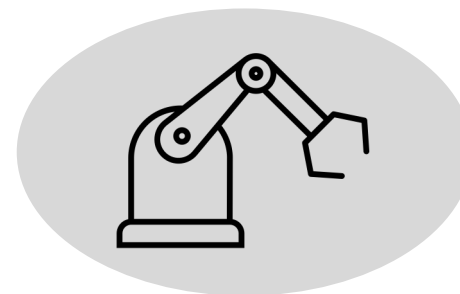
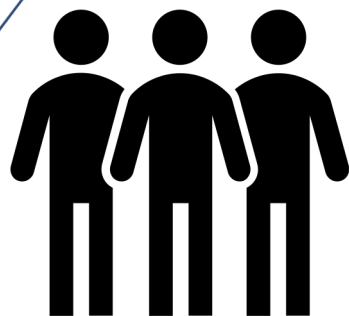
Demonstration



Ranking



Bobu et al. TRO'20
Biyik et al. IJRR'20



Inverse Specification

Interact with human to better understand their preference



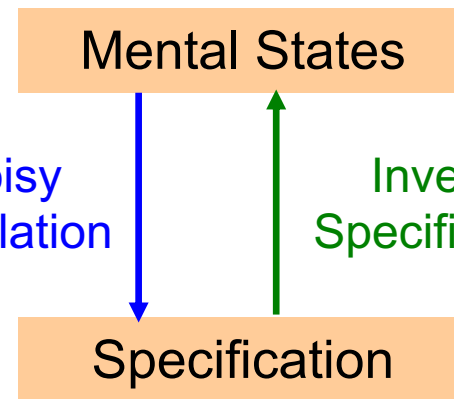
send queries to human and receive their ranking feedback



(1) components of objective
(2) constraints

Noisy translation

Inverse Specification

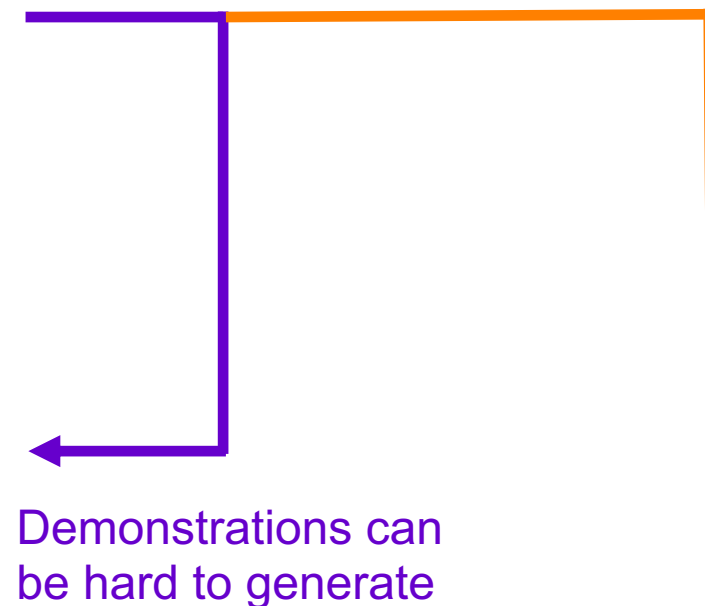


Previous Works – inverse reinforcement learning / inverse optimal control

- Maximum Entropy IRL [Ziebert et al. AAAI'08]
 - Based on demonstrations
 - The trajectory distribution only relies on the human utility
 - $P_{w_H}(q_i) \propto \exp(u_{w_H}(q_i))$, u_{w_H} : human utility

- IRL by human preferences [Christiano et al. NeurIPS'17]
 - Given a query, $\mathbf{q} := (q_i, q_j)$
 - Provide feedback (f): $q_i > q_j, f = [1, 0]^T$; else, $f = [0, 1]^T$
 - Loss: $L = -\sum f[0] \log P_w(\text{pick } q_i) + f[1] \log P_w(\text{pick } q_j)$

- Constraint inference for IRL [Scobee et al ICLR'20]
 - Assume nominal reward (\tilde{w}) and N available demonstrations (Q_D)
 - Maximize $P(C) = \frac{1}{Z(C)^N} \prod_{q \in Q_D} \exp(u_{\tilde{w}}(q)) \mathbb{1}_C(q)$



Preference by reward and constraint is more succinct

Overall Structure

- **Inverse specification**

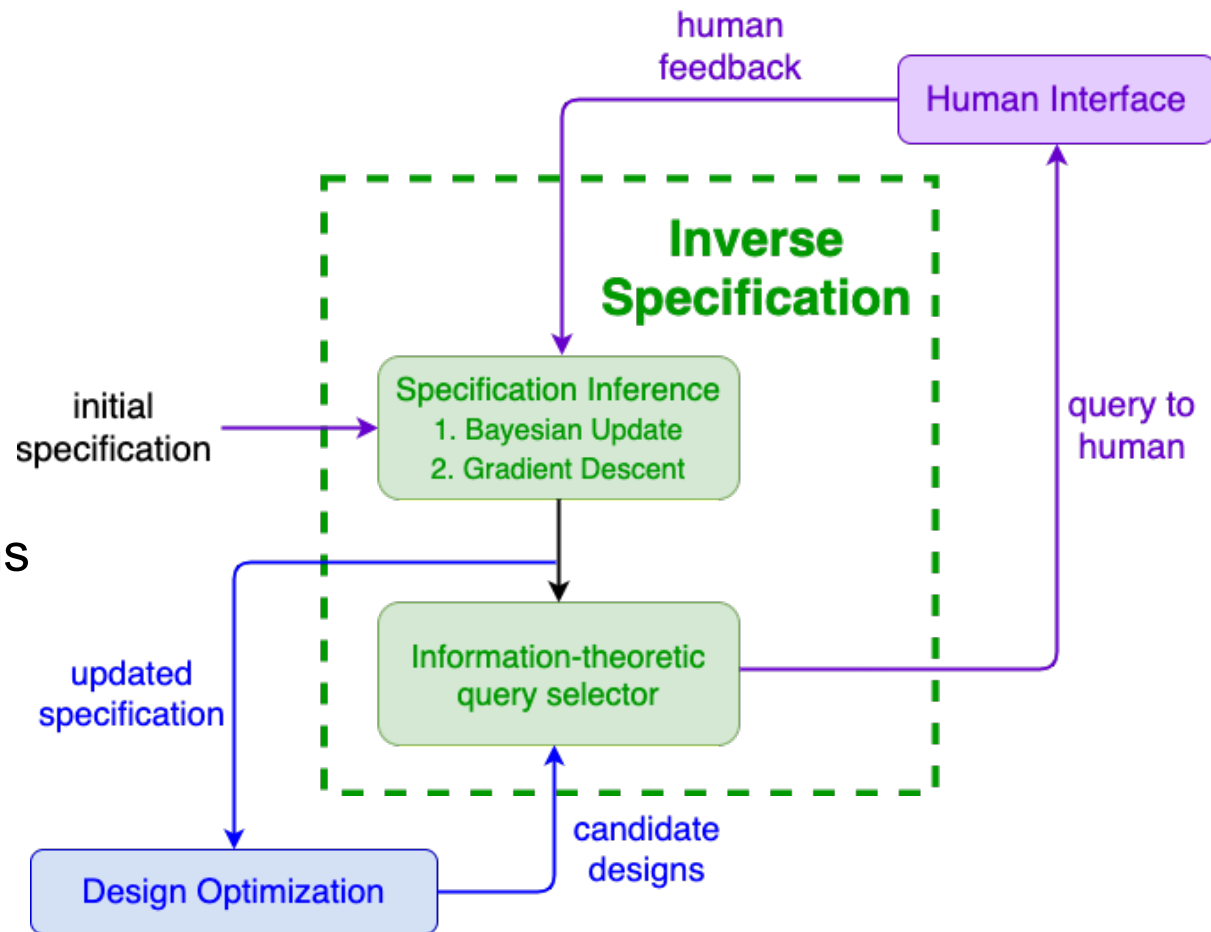
- We interact with humans to refine the problem specification and accelerate exploration

- **Design optimization**

- We pick candidate designs by genetic algorithms or trained policies by reinforcement learning

- **Human interface**

- We pick informative queries from the candidate designs or trajectories



Experiment Details

- Human preference
 - $P_{\mathbf{w}_H, \mathcal{C}}(\text{pick } q_i) \propto \exp(u_{\mathbf{w}_H}(q_i)) \cdot \mathbb{1}_{\mathcal{C}}(q_i)$
- Human model in inverse specification machinery
 - $P_{\mathbf{w}, \theta}(\text{pick } q_i) \propto \exp(u_{\mathbf{w}}(q_i)) \cdot h_{\theta}(q_i)$
- Design space
 - Each design: $q \in \mathbb{R}_+^6$
 - The true optimal design is obtained by

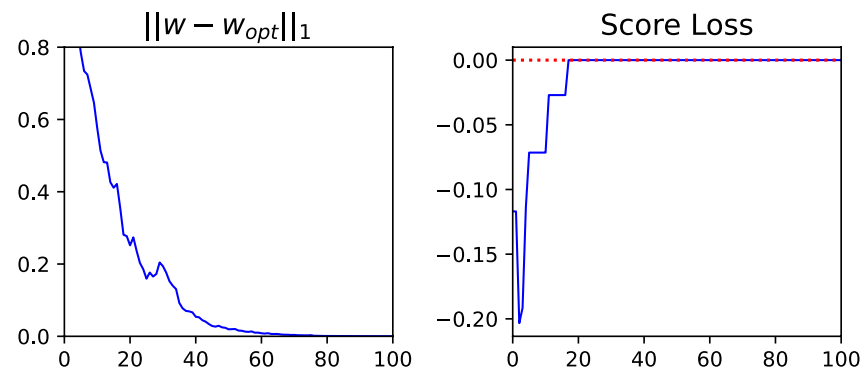
$$\arg \max_q \mathbf{w}_H^T q \cdot \mathbb{1}_{\mathcal{C}}(q)$$
 - The predicted optimal design is obtained by

$$\arg \max_q \mathbf{w}^T q \cdot h_{\theta}(q)$$

Infer utility, assume no explicit constraints

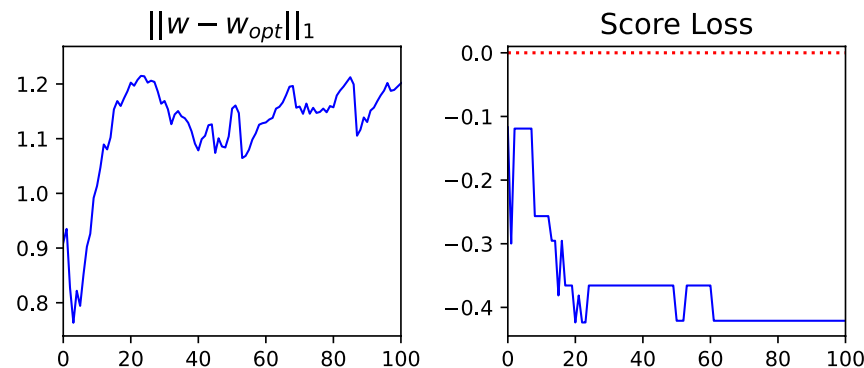
- Bayesian Update: $P(\mathbf{w} \mid \mathbf{q}, f) \propto P(f \mid \mathbf{q}, \mathbf{w}) \cdot P(\mathbf{w})$

no hard constraints



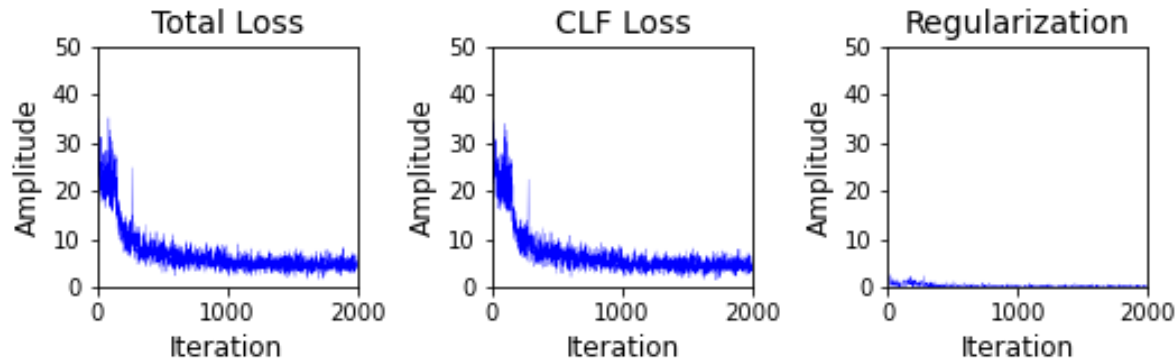
- Constraint-agnostic inferred utility over-emphasizes constrained features.

one hard constraint



Infer constraints, given proxy utility

- $L(\theta) = \sum_{(q,f) \in B} \text{KL}(P_{\theta}(q) || f) + \alpha \text{Reg}(\theta)$
 - Gradient descent on neural network parameters (θ)



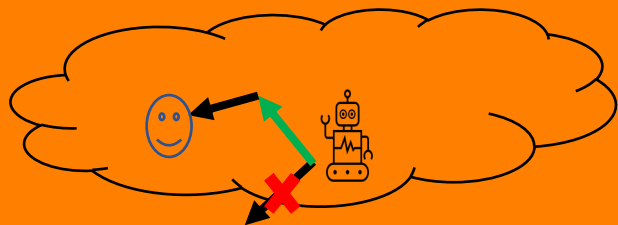
- Feasible designs but classified infeasible: 4.3%
- Infeasible designs but classified feasible: 0%
- Predict top designs by: $\arg \max_q u_w(q) \cdot h_{\theta}(q)$
 - Predicted top-5 designs: [133 23 45 114 173]
 - Real top-5 designs: [133 23 45 114 173]

Future Works

- Infer the utility and constraint simultaneously
 - Alternating gradient descent: $v_{w, \theta}(q) = u_w(q) \cdot h_{\theta}(q)$
- Active learning: how to select the most informative queries to present to the human designer
 - Information gain
 - What is the analog metric?

Key Takeaways

Supervisory Control



- Discounted reach-avoid Bellman equation enables reinforcement learning to solve HJ PDE
- We treat the policy as untrusted oracles and employ a shielding scheme → Learned policy is the best-effort reach-avoid policy

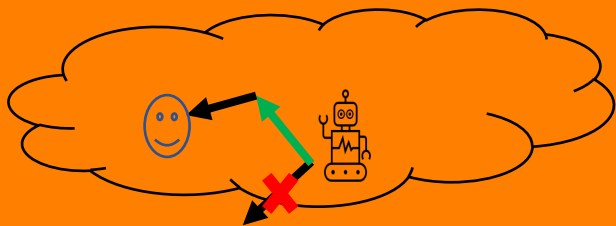
Inverse Specification



- Separating constraints from components of objective function makes the problem easier
- We can infer constraints by querying human a pair of designs and receiving ranking feedback

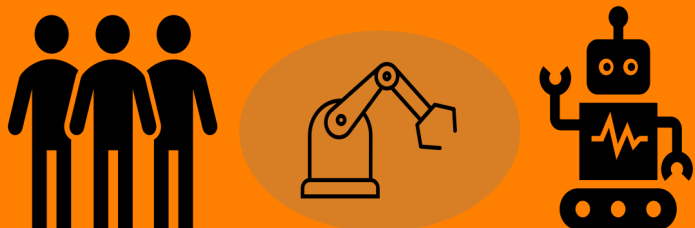
Future Works

Supervisory Control



- How to separate the action policy and reach-avoid value function?
- How to use RL to solve zero-sum reach-avoid differential game?
- How to use shielding scheme to improve PAC-Bayes bound on novel environments?

Inverse Specification



- How to infer utility and constraint together?
- How to select the most informative queries to present to the human designer?

Reference

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